Identification and reconstruction of low-energy electrons in the ProtoDUNE-SP detector

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Measurements of electrons from $\nu_e$ interactions are crucial for the Deep Underground Neutrino Experiment (DUNE) neutrino oscillation program, as well as searches for physics beyond the standard model, supernova neutrino detection, and solar neutrino measurements. This article describes the selection and reconstruction of low-energy (Michel) electrons in the ProtoDUNE-SP detector. ProtoDUNE-SP is one of the prototypes for the DUNE far detector, built and operated at CERN as a charged particle test beam experiment. A sample of low-energy electrons produced by the decay of cosmic muons is selected with a purity of 95%. This sample is used to calibrate the low-energy electron energy scale with two techniques. An electron energy calibration based on a cosmic ray muon sample uses calibration constants derived from measured and simulated cosmic ray muon events. Another calibration technique makes use of the theoretically well-understood Michel electron energy spectrum to convert reconstructed charge to electron energy. In addition, the effects of detector response to low-energy electron energy scale and its resolution including readout electronics threshold effects are quantified. Finally, the relation between the theoretical and reconstructed low-energy electron energy spectra is derived, and the energy resolution is characterized. The low-energy electron selection presented here accounts for about 75% of the total electron deposited energy. After the addition of lost energy using a Monte Carlo simulation, the energy resolution improves from about 40% to 25% at 50 MeV. These results are used to validate the expected capabilities of the DUNE far detector to reconstruct low-energy electrons.

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I. INTRODUCTION

Discoveries over the past half-century have positioned neutrinos, one of the most abundant matter particles in the Universe, at the center stage of fundamental physics. Neutrinos are now being studied to answer open questions about the nature of matter and the evolution of the Universe. In particular, the measurement of $CP$ violation in the lepton sector [1,2] will help probe the possibility that early-Universe $CP$ violation involving leptons might have led to the present dominance of matter over antimatter. DUNE [3,4] is a next-generation long-baseline accelerator neutrino experiment, designed to be sensitive to neutrino oscillations. The DUNE experiment will consist of a far detector [5] to be located about 1.5 km underground at the Sanford Underground Research Facility (SURF) in South Dakota, USA, at a distance of 1300 km from Fermilab, and a near detector [6] to be located at Fermilab. DUNE uses liquid argon time projection chamber (LArTPC) technology, which permits the reconstruction of neutrino interactions with mm-scale precision. $CP$ violation will be tested in $\nu_\mu \to \nu_e$ oscillations and the corresponding anti-neutrino channel, which are sensitive to the $CP$-violating phase and the neutrino mass ordering [7]. In addition, the large underground LArTPC detectors planned for DUNE will enable a rich physics program beyond the accelerator-based neutrino oscillation program, including searches beyond the standard model [8], supernova neutrino detection [9], and solar neutrino measurements [10].

To achieve the planned DUNE physics program, it is critically important to accurately reconstruct the energies of electrons and positrons originating from MeV-scale solar and supernova burst $\nu_e$’s as well as GeV-scale neutrinos from the Long-Baseline Neutrino Facility beam. Calorimetric energy reconstruction requires efficient charge collection, calibration corrections to account for liquid argon impurities and electronics response, and a recombination correction to account for charge loss due to electron-ion recombination. The goal of this article is to demonstrate the capability to reconstruct low-energy electrons in the single-phase ProtoDUNE (ProtoDUNE-SP) [11] LArTPC. This work presents techniques and results on the selection and energy reconstruction of the low-energy (Michel)
electrons [12], originating from the decay at rest of cosmic ray muons. With a well-understood energy spectrum, these low-energy electrons are ideal for evaluating the electron selection and energy reconstruction in ProtoDUNE-SP and demonstrating the capability of the DUNE far detector to identify and reconstruct these low-energy electron events. Although there are other studies of low-energy electrons in LArTPCs [13–17], the unique features of this study include the data-driven determination of the recombination correction, evaluation of the lost energy due to the TPC readout threshold, a comparison of the electron energy calibration based on muon-derived calibration corrections with that based on the Michel electron true energy spectrum, and a characterization of the electron energy resolution.

II. DUNE FIRST FAR DETECTOR AND ITS PROTOTYPE

Central to the realization of the DUNE physics program is the construction and operation of LArTPC detectors that combine a many-kiloton fiducial mass necessary for rare-event searches with the ability to image those events with mm-scale spatial resolution, providing the capability to identify the signatures of the physics processes of interest. The DUNE far detector will consist of four detector modules, each with an equivalent LAr fiducial mass of 10 kt, installed approximately 1.5 km underground. Each LArTPC will be installed inside a cryostat of internal dimensions $15.1 \, \text{m} \times 14 \, \text{m} \times 62 \, \text{m}$ containing a total LAr mass of about 17.5 kt. Charged particles passing through the TPC ionize the argon, and the ionization electrons drift to the anode planes under the influence of an applied electric field.

DUNE is actively developing two LArTPC technologies: a horizontal-drift (HD) LArTPC in which the ionization electrons drift horizontally between a vertical cathode and anode planes, and a vertical-drift LArTPC, in which the ionization electrons drift vertically between a horizontal cathode and anode planes. The focus of this article is on the HD LArTPC [18] technology as the first DUNE far detector module will be based on this technology.

Figure 1 (top) shows the configuration of a DUNE HD module. Each of the four LAr drift volumes is subjected to an electric field of $500 \, \text{V/cm}$ [19], corresponding to a Cathode Plane Assembly (CPA) high voltage of $-180 \, \text{kV}$ relative to the anode, which will be grounded. The pattern of ionization collected on the grid of anode wires enables reconstruction in the two coordinates perpendicular to the drift direction. Novel photon detectors (PDs) called X-ARAPUCAs [20] will be placed behind the Anode Plane Assembly (APA) collection wire planes. The PDs are used to provide a timestamp of the interaction, thus giving an estimate of the drift distances traveled by the ionization electrons to reconstruct the third event coordinate.

The DUNE Collaboration has constructed and operated a large horizontal drift prototype detector, known as ProtoDUNE-SP. The detector has been assembled and tested at the CERN Neutrino Platform [21]. ProtoDUNE-SP was operated from 2018 to 2020, and its large samples of high-quality beam data have been used to demonstrate the effectiveness of the single-phase far detector design. Results on the performance of the ProtoDUNE-SP liquid argon TPC in the test beam can be found in Ref. [22] including noise and gain measurements; $dE/dx$ calibration for muons, protons, pions, and electrons; drift electron lifetime measurements; and photon detector noise, signal sensitivity, and time resolution measurements. The measured values meet or exceed the specifications for the DUNE far detector. Figure 1 (bottom) shows the components of the ProtoDUNE-SP LArTPC, which is approximately one-twentieth the size of the planned far detector HD module but uses anode and cathode components identical in size to those of the full-scale module. ProtoDUNE-SP has the same 3.6 m maximum drift length as the full far detector HD module. It consists of two drift volumes with a common central cathode surrounded by two anode planes and a field cage that surrounds the entire active volume. The active volume is 6 m high.
Each anode plane consists of three adjacent APAs that are each 6 m high by 2.3 m wide. The wire planes and their wire orientations are the U layer (+35.7° from vertical, also called the first induction plane), the V layer (−35.7° from vertical, also called the second induction plane), and the X layer (vertical, also called the collection plane). Each successive wire plane is built 4.75 mm above the previous layer. As they drift, ionization electrons first pass the induction planes and then are collected on the collection plane. The U and V plane wires are wrapped around the APA frame (and hence see the charge arriving from both sides of the APA) while each side has a separate X layer, as sketched in Fig. 3 of [22]. The distance between two consecutive wires in the same layer, also known as wire pitch, is 4.67 mm for U and V layers, and 4.79 mm for X layer wires. Signals from the wires of each APA are read out via a total of 2560 electronic channels.

Uniformity of the electric field is provided by the surrounding field cage. The cold electronics mounted onto the APA frame, and thus immersed in LAr, amplify and continuously digitize the induced signals on the sense wires at 2 MHz during the entire data-taking period, and transmit these waveforms to the Data Acquisition system. The modular PD system is integrated into the APAs, as further described in [22]. The PD was not used in the analysis described here.

III. ELECTRONS IN LARTPCS

For the DUNE physics program it is critical to understand the far detector response to electromagnetic showers since DUNE will measure electrons produced in ν_e interactions, where the ν_e are from ν_μ oscillations, the Sun, and possibly supernova explosions. In addition, DUNE will search for proton decay signatures, as event identification may proceed via the detection of a low-energy electron. ProtoDUNE-SP has collected data samples of test-beam electrons and data samples of electrons from cosmic ray muon decays [22]. Data from ProtoDUNE-SP beam runs with 1 GeV/c beam momentum, including a sample of beam positrons, were used for the initial classification of track- and showerlike energy deposits using a convolutional neural network technique [23]. Studies of electron selection and identification in ProtoDUNE-SP TPC lead to a more accurate understanding of the calorimetric response to electrons and offer an opportunity for a precise understanding of the electron energy resolution parameters for electron neutrino reconstruction in future DUNE far detectors. This work focuses on studies of the ProtoDUNE-SP LArTPC response to low-energy electrons.

As the electrons propagate in the LAr, they deposit energy either through ionization or through radiative losses (bremsstrahlung). The energy loss via ionization is continuous and results in tracklike topologies. Radiative losses are also present at all electron energies leading to the production of electromagnetic shower cascades of secondary electrons and photons. Bremsstrahlung photons may Compton scatter or convert to e^+e^- pairs, resulting in signatures with secondary energy deposits disconnected from the primary ionization tracks. The typical attenuation length for photons in liquid argon in the energy range of interest for Michel electrons is 20–30 cm [24]. The event reconstruction takes into account the charge released by both primary particle ionization and radiative processes.

IV. SELECTION OF STOPPING MUONS AND MICHEL ELECTRONS

The generation of cosmic ray muons is performed with CORSIKA v7.4 [25], while the simulation of particle propagation and interaction in ProtoDUNE-SP is performed by GEANT4 v4.10.3 by using the QGSP BERT physics list [26] with the detector response described within LArSoft [27]. In all ProtoDUNE simulations, the delta-ray threshold (and the electron transport threshold) is set to 455 keV (corresponding to an electron range of about 1.5 mm) [28]. All μ^- decay into Michel positrons, whereas only 25% of μ^- undergo decay to Michel electrons since the other 75% are captured by the argon atoms inside the TPC. Therefore, the Michel electron sample described in this analysis includes both electrons and positrons. In this article, “electrons” refers to both electrons and positrons unless indicated otherwise.

The reconstruction of charged particles in the ProtoDUNE-SP LArTPC follows the technique described elsewhere [22], and in this section the procedure is briefly described. The TPC readout electronics collect a waveform that represents the current on the APA wire as a function of time. Each waveform is processed in an offline data processing chain to produce a collection of ionization charge deposition arrival times and charge integrals at each readout wire. Signal processing starts with a deconvolution of measured charge from signals induced by the drifting ionization electrons, followed by noise removal. In order to make use of deconvolved waveforms to reconstruct individual events, it is necessary to apply three-dimensional (3D) hit finding and pattern recognition algorithms. The 3D-hit (called “hit” from now on) is an ionization charge released in space and time by through-going charged particles and detected by three layers of anode plane wires, and collected by a collection plane wire alone in the analysis described here. A collection of hits is merged together to form a particle track or a shower that belongs to an event. The hit finding algorithm searches for candidate hits based on charge deposits in the waveform on a single wire as a function of time, and fits them to a Gaussian shape. Pattern recognition and event reconstruction are performed by the PANDORA software package [29], which is...
a collection of reconstruction algorithms that focus on specific hit topology patterns. The first step in the reconstruction procedure is the two-dimensional clustering of observed charge pulses in each of the three detector readout planes separately. In the second step, sets of two-dimensional clusters are matched between the three views to produce 3D hits and to create particle interaction hierarchies. As described in [22], one important feature of the cosmic ray reconstruction step is the “stitching” of tracks across the boundaries between neighboring drift volumes bounded by a CPA or an APA. In the analysis performed here the stitching procedure is applied when two 3D clusters are reconstructed in neighboring drift volumes with consistent direction vectors and an equal but opposite shift in the drift direction from the CPA. When the clusters are shifted toward each other as expressed in time-tick units (1 time tick = 500 ns), a single muon track of two initially separate tracks is produced with a known absolute position and time \( T_0 \) relative to the trigger time [22].

The reconstruction of electrons below 50 MeV is very different from the reconstruction of GeV-scale electromagnetic showers [30]. For this reason, a dedicated algorithm has been developed to reconstruct and identify the Michel electrons presented in this study. Figure 2 shows two Michel electron candidate events from ProtoDUNE-SP data, with muons entering from the top.

The event selection starts by searching for a candidate muon that decayed to an electron. A set of conditions is initially applied to ensure a high quality muon track candidate. Finally, additional selection criteria are implemented to make sure that a Michel electron candidate is identified around the end position of the candidate muon by selecting and summing up charge hits that represent the Michel electron. While all three anode planes are used for track reconstruction, the collection plane provides the best signal-to-noise performance and charge resolution [22]. Therefore, only the collection plane charge is used to reconstruct the electron energy.

### A. Muon track selection

(i) Only the \( T_0 \)-tagged candidate muon tracks are selected from muon tracks reconstructed by PAN-DORA. These are the tracks that cross the cathode or anode plane boundaries, and the two pieces of the track from the two volumes help determine the correct end position of the track in the drift direction. The fraction of tracks having a \( T_0 \) assigned to them is 2% from the data sample. Since this requirement selects most of the events and the corresponding charge coming from locations farther away from the anode in ProtoDUNE-SP, it is expected that the DUNE far detector will perform equally or better in terms of charge reconstruction. This is because there will be less ionization charge attenuation as events, on average, will be closer to the anode plane wires and that may slightly affect the energy reconstruction.

(ii) Selected tracks are required to have one reconstructed endpoint within 30 cm from one or more of the detector boundaries. The cut is applied to all six faces of the detector. This step improves the selection of cosmic ray muon candidates entering the detector. By requiring this, the next steps in the selection can focus on the other end of the track to search for the Michel electron signatures.

(iii) Only the muons that stop within the detector fiducial volume are considered. The fiducial volume is a rectangular volume shaped as follows: the boundary from the anode planes is 51 cm, the boundary from the upstream and downstream ends is 80 cm, and the boundaries from the top and bottom of the TPC are 43 cm and 80 cm, respectively. These values are obtained from an optimization based on Monte Carlo (MC) simulation. This step specifies the end of the contained track from which evidence of Michel electrons can be sought.

(iv) Muon tracks that stop within a region that is close to a boundary between two adjacent APAs (~10 cm from each APA side) are removed. This cut removes all those tracks that appear to stop in the gaps between two APA planes.
(v) Broken tracks, for which the reconstruction algorithm does not connect track segments correctly at detector boundaries or anode gaps, are removed from further analysis. In order to reject broken candidate muon tracks, the algorithm looks for any additional track that starts within $<30\text{ cm}$ of the reconstructed end position of the candidate muon track, and is nearly parallel ($<14^\circ$ or $>165^\circ$) with respect to the candidate muon track. If this condition is satisfied, the candidate muon is removed from the event selection.

(vi) It is required that candidate muon tracks are at least $75\text{ cm}$ long [31], i.e., those that have crossed the cathode with track segments reconstructed in both drift volumes. Since cosmic muons generally have long track lengths, this cut improves the quality of the candidate cosmic muon track reconstruction.

(vii) Every reconstructed hit is associated with a time counted in ticks, known as the hit time with respect to $T_0$. The peak of the reconstructed hit time distribution is known as the hit peak time. For every track, a cut is placed on the value of the minimum and maximum hit peak time. Only those candidate muon tracks that have a minimum hit peak time to be $>200$ time ticks and a maximum hit peak time to be $<5800$ time ticks are kept. The peak time cuts ensure that the candidate muon is contained within the event readout window.

About 28% of the $T_0$-tagged muons satisfy the above selection criteria, and simulation studies indicate that the selected muon sample has a purity of 99.7%. The purity here corresponds to the fraction of the true muons out of all the selected tracks. The determination of the selection cut values for different quantities is based on the MC simulation studies for which the maximum sample purity is obtained.

B. Michel electron selection

(i) The first step in the identification of Michel electrons is to select nearby hits, i.e. hits within 10 cm of the end position of the candidate muon. In the collection plane view, these hits must not belong to either the candidate muon or any other track having length $>10\text{ cm}$. Nearby hits are counted, and events that have between 5 and 40 hits around the endpoint of the candidate muon track are considered. These values are optimized to deliver a high sample purity. Furthermore, the reconstructed electron shower around the candidate muon track endpoint is required to start within 10 cm from the candidate muon track end position. The Michel electron candidate is formed from these selected electron shower hits.

(ii) The direction of the candidate Michel electron (obtained by a linear fit to the nearby hits) is compared to the direction of the muon (measured using the last 10 hits in the trajectory). The angle between the directions is required to be less than $130^\circ$ such that events where the candidate Michel electron goes back along the muon are rejected.

(iii) In the next step, the angle between the collection plane wires and the direction of the candidate Michel electron is calculated. Only those events where the value of this angle is $>10^\circ$ and $<170^\circ$ are selected so that Michel electron candidates that are parallel to the collection plane wires are not included in the data sample. This cut is applied to reject Michel electrons that are parallel to the collection plane wires and therefore may not have well-reconstructed hits.

(iv) The final selection criterion, the cone cut, separates Michel electron hits from nearby cosmic rays that may interact in the TPC close to the candidate Michel electron event. A cone around the endpoint of the candidate muon is defined such that any hit that lies within that cone is assumed to belong to the candidate Michel electron. It is required that those hits are not a part of the parent muon or any other track longer than 10 cm. A straight line is fit along the nearby collection plane hit distribution (hits within 10 cm distance from the muon endpoint in the collection plane). The cone cut is illustrated in Fig. 3, where the red points represent the Michel electron hits, and the black points are other (non-Michel candidate) hits of the event excluding the hits of the parent muon or any other long ($>10\text{ cm}$) tracks. Using simulation, the cone opening angle $\theta$ is optimized at $70^\circ$ and the cone length $d$ is 20 cm in order to maximize the value of Michel electron hit purity (83%) and hit completeness (74%). The hit purity is defined as the fraction of hits in the reconstructed cone that actually belong to the true Michel electron. The hit completeness is defined as the fraction of true Michel electron hits inside the reconstructed cone.

![FIG. 3. Illustration of the cone containment that separates Michel electron hits (red dots) from nearby cosmic ray background events (black dots). The Michel electron is defined by the hits starting within 10 cm from the end position of the candidate muon. All the hits contained inside the cone cuts are taken to be the candidate Michel electron hits.](image-url)
TABLE I. Passing rates for event selection criteria applied to ProtoDUNE simulation and data samples. Quantities with statistical uncertainties for muon selection present the percentage with respect to well-reconstructed muons. Quantities with statistical uncertainties for Michel electron selection present the percentage with respect to well-reconstructed muons that satisfy the muon selection criteria.

<table>
<thead>
<tr>
<th>Passing rates</th>
<th>Simulation</th>
<th>Data</th>
</tr>
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<tbody>
<tr>
<td>Muon selection</td>
<td>(27.9 ± 0.1)%</td>
<td>(25.5 ± 0.1)%</td>
</tr>
<tr>
<td>Michel electron selection</td>
<td>(16.3 ± 0.1)%</td>
<td>(14.5 ± 0.2)%</td>
</tr>
</tbody>
</table>

C. Event selection summary

Table I lists the muon passing rates and corresponding statistical uncertainties with respect to the well-reconstructed muon tracks and candidate Michel electrons passing rates with respect to the well-reconstructed muons that satisfy the muon selection criteria for the simulation and data samples. As the focus of this analysis was to select a pure sample of Michel electrons, an estimation of the systematic uncertainties on the passing cosmic ray muon rates was not performed here. The total number of data events in this study that pass all the selection steps is ∼8300. The total event purity of the selected electron sample from the simulation is found to be 95%. The purity here corresponds to the fraction of the true Michel electron events out of all the selected events. The remaining 5% of events represent different types of background events including those that have a tagged electromagnetic activity from muons (delta rays or bremsstrahlung photons), in which some random noise hits appear to be reconstructed as candidate Michel electron hits or those in which protons are emitted from argon nuclei because of the muon capture on argon. Isolating background events in the simulation, their energy spectrum is found to be monotonically decreasing, with a low-end cutoff at ∼10 MeV. These secondary background events have been characterized elsewhere [30,32].

It is important to point out that the DUNE far detector data will be dominated by single νμ or single νe events, where the event selection and reconstruction efficiencies will improve in the absence of nearby cosmic ray background activity, as opposed to the ProtoDUNE-SP case studied in this article. It is expected that the muon flux inside ProtoDUNE-SP is on the order of one per cm²/min [33]. The event selection criteria will be revisited and optimized for the DUNE far detector analyses. An expected muon rate in four modules of DUNE being underground will be about 0.2 Hz with an average muon energy of 283 GeV [34].

V. TEST AND VERIFICATION OF THE MICHEL ELECTRON RECOMBINATION CORRECTION

A through-going charged particle will deposit energy in LAr by creating both ionization and excitation. Electron-ion pairs will be produced (e−, Ar+), along with excited argon atoms (Arx). These excited atoms (Arx) will form excited molecular argon ions, so-called short-lived excimers (Arx3), through collisions of Ar+ with neutral Ar atoms. In addition, the Arx3 will also be formed by free electrons recombining with surrounding molecular argon ions (Arx+). These excimers (Arx3) undergo dissociative decay to their ground state by emitting the vacuum ultraviolet photons known as argon scintillation light [14,32,35]. When the deposited energy is reconstructed using charge alone, as done in the work presented here, only the electrons that escape electron-ion recombination and successfully drift to anode collection wires will be accounted for. Note that R is the recombination factor that describes the fraction of ionization electrons that survive prompt recombination with argon ions before the drift towards the anode plane. The value of R is critical to energy reconstruction from collected ionization charge, as later described in Eq. (3). In this subsection the data-driven recombination correction factor is derived by following the Modified Box model [36]. The Michel electron candidates in this study are selected with the cuts described in Sec. IV B. The electron energy loss per unit length is calculated on an event-by-event basis. The value of dQ/dx per event is computed as

\[ dQ/dx = \frac{Q_{\text{total}}}{L}, \]

where \( Q_{\text{total}} \) is the total charge deposited determined from the candidate Michel electron hits and \( L \) is the 3D displacement from the first to the last hit of the candidate Michel electron. In both data and MC, raw \( dQ/dx \) is converted to corrected \( dQ/dx \) based on calibration constants derived with the cosmic ray muons [22], as described later by Eq. (3). With the Modified Box model [36], the calibrated \( dQ/dx \) value is converted to an average \( dE/dx \) for every Michel electron candidate. The average \( dE/dx \) distribution of Michel electron candidates is shown in Fig. 4 (top). The mean value of the \( dE/dx \) distribution is 3.25 MeV/cm. Finally, the agreement of simulation with data is tested using the recombination correction factor distribution. The recombination factor \( R \) is calculated as

\[ R = \frac{\ln \left( \frac{dE}{dx} \times \beta' / \rho E_f + \alpha \right)}{\ln \left( \frac{dE}{dx} \times \beta' / \rho E_f + \alpha \right)}, \]

where \( \alpha \) and \( \beta' \) are the Modified Box model parameters which were measured by the ArgoNeuT experiment at an electric field strength of 0.481 kV/cm [36]. The values of \( \alpha \) and \( \beta' \) are 0.93 ± 0.02 and 0.212 ± 0.002 (kV/cm)(g/cm²)/MeV, respectively. The liquid argon density \( \rho \) at a pressure of 124.11 kPa is 1.38 g/cm³, and \( E_f \) is the applied electric field. Using Eq. (2), \( R \) is computed for each event using \( dE/dx \) for the event and assuming a constant electric field of 0.5 kV/cm [19]. The \( R \) distribution of Michel electron candidates is shown in Fig. 4 (bottom).
The mean values of the recombination factor obtained from the reconstructed data and MC distributions in Fig. 4 (bottom) are

\[ 0.625 \pm 0.020 \text{(stat)} \] and \[ 0.626 \pm 0.020 \text{(stat)} \], respectively. Independent of the analysis performed above, the average recombination factor of \( 0.644 \pm 0.014 \text{(syst)} \) was evaluated based on the ProtoDUNE-SP GEANT4 electron simulation [26], which incorporates the Modified Box model of the ionization electron recombination and its systematic uncertainty as described in [36]. The recombination factor \( R = 0.644 \) derived with the simulation comes with a small uncertainty and agrees well with the data-driven value described in this subsection, verifying the simulation-based recombination factor applied in the analysis described in this article.

VI. MICHEL ELECTRON LOST ENERGY STUDIES

The lost energy is a fraction of energy that is not reconstructed. It corresponds to ionization charge deposits that are missed by either being left below the anode charge readout threshold or left outside the selection cone. This subsection describes the Michel electron lost energy studies performed to quantify the containment of Michel electron events within the applied cone cut and to evaluate the effects of TPC readout thresholds using MC simulation.

A. Michel electron hit completeness

Figure 5 shows the fraction of true Michel electron energy left outside the cone as a function of true Michel electron energy per event. The average value of the energy loss due to hit incompleteness for the Michel electron sample is \( 13 \pm 1 \text{(stat)} \)%. It is also evident that the energy loss by hits not captured within the reconstruction cone increases with the Michel electron energy due to the increase of radiative losses.

B. Michel electron hit reconstruction threshold

In order to avoid random noise from being reconstructed as a particle hit, there is an intrinsic threshold applied to the energy deposited in a given readout channel (wire) per time tick, the value of which is set to \( \sim 100 \) keV/tick. To quantify the impact of the threshold on the Michel electron energy distribution, a study was performed to look at all simulated channels and to estimate the lost energy due to the above-mentioned threshold. Figure 6 shows the true Michel electron lost energy fraction as a function of true Michel electron energy per event from this threshold; on average...
11 \pm 1 \text{(stat)}\% of the ionization from Michel electrons is lost due to this threshold.

Therefore, a total of about 24\% of the true energy is not reconstructed from hits outside the cone and below threshold, so only 76 \pm 1 \text{(stat)}\% of the total energy is captured.

VII. MICHEL ELECTRON ENERGY RECONSTRUCTION

This section describes the procedure of Michel electron energy reconstruction. In the first method (also called nominal reconstruction) cosmic ray muon data are used to derive calibration constants and corrections [22], which are then applied to reconstructed Michel electron hits. The second approach is based on the well-understood theoretical Michel electron energy spectrum [12] where the energy calibration is independent of the muon-based calibration. Finally, the energy resolution effects important for understanding the electron energy in the 5–50 MeV range in LArTPCs are discussed. It should be clarified that the nominal energy reconstruction presented here does not include the lost energy because it cannot be captured in the data with the existing event selection and charge readout threshold. However, potential energy reconstruction improvements with some or all of the lost energy recovered are studied with the simulation to indicate opportunities that might be realized with future DUNE far detector LArTPCs.

A. Muon-based energy reconstruction of the Michel electron energy scale

The electron energy, $E$, is calculated from the sum of charges deposited by the corresponding ionization electron hits on the anode plane wires. The total reconstructed energy of the Michel electron is given as

$$E = \frac{C_{\text{norm}} \cdot W_{\text{ion}}}{R \cdot C_{\text{calib}}} \cdot \sum_{i=1}^{N} [e(X_i) \cdot e(Y_i, Z_i) \cdot dQ_i] \quad (3)$$

where $dQ_i$ (in ADC tick) corresponds to the charge deposited in the $i$th hit, and $N$ corresponds to the total number of candidate Michel electron hits. Note that $dQ_i/dx$ values along the drift direction are affected by attenuation due to electronegative impurities and by longitudinal diffusion. Here, $C_{\text{norm}}$ is the factor that normalizes the reconstructed $dQ_i/dx$ values to the average $dQ_i/dx$ value across anode planes in both drift volumes; $e(X_i)$ represents the drift electron lifetime and the space charge corrections, and $e(Y_i, Z_i)$ describes the dead wire correction that is used to remove the nonuniformity in $dQ_i/dx$ values [22]. In addition, $W_{\text{ion}}$ (= 23.6 eV) is the ionization work function of argon [37]. A highly pure sample of stopping muons is used in ProtoDUNE to correct for space charge effects and to determine $dQ_i/dx$ [22]. From the calibrated $dQ_i/dx$ values (in ADC/cm) along the muon track in its MIP region, the $dE/dx$ (in MeV/cm) values are fitted using the Modified Box model [36] function to correct for the recombination effect with the charge calibration constant $C_{\text{calib}}$ as a free parameter in the $\chi^2$ minimization. Therefore, $C_{\text{calib}}$ (ADC tick/electron) represents the calibration constant that is used to convert the corrected charge deposition (in ADC) on a hit to energy deposition (in MeV) on a hit. It accounts for the electronics gain of the collection-plane wires, the signal processing, as well as detector effects that convert the deposited energy into collected electrons on the wire planes. Note that $R = 0.644$ is the average recombination correction evaluated by the ProtoDUNE-SP GEANT4 simulation based on the Modified Box model [36], and it is verified above on an event-by-event basis by selected Michel electron events. The reconstructed Michel electron energy is evaluated on an event-by-event basis using Eq. (3) in which all the calibration corrections are derived from cosmic ray muon data and simulation samples. Therefore, the energy reconstruction applied to the Michel electron sample in this subsection is based on cosmic ray muon calibration.

With the Michel electron energy reconstruction described in Eq. (3), it is appropriate to evaluate systematic uncertainty contributions to the energy scale. These contributions originate from charge hit ($dQ_i$) association efficiency, the recombination factor ($R$) uncertainty, the theoretical Michel electron versus positron uncertainty, and from the space-charge effects [$e(X_i)$] uncertainty. These uncertainties quantify how well the absolute energy scale of Michel electrons is understood. Systematic uncertainty contributions from $C_{\text{calib}}$, $e(Y_i, Z_i)$ and $C_{\text{norm}}$ are negligible. Table II presents the systematic uncertainties on the reconstructed Michel electron energy spectrum. The uncertainties are expressed with respect to the mean energy of the reconstructed Michel electron energy spectrum. Individual contributions are added in quadrature.

The hit association systematic uncertainty was evaluated by considering the number of candidate Michel electron hits within 10 cm of the muon stopping point in both data and simulation. The difference in the average number of hits in data and simulation was used to vary the MC Michel electron hit distribution. A shift in the mean value of the reconstructed Michel electron energy scale was determined.

<table>
<thead>
<tr>
<th>Sources of systematic uncertainties</th>
<th>Uncertainty estimates</th>
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<tr>
<td>Hit association efficiency</td>
<td>4.0%</td>
</tr>
<tr>
<td>Recombination factor</td>
<td>2.2%</td>
</tr>
<tr>
<td>Michel electron versus positron</td>
<td>1.7%</td>
</tr>
<tr>
<td>Space charge effect</td>
<td>1.4%</td>
</tr>
<tr>
<td>Total added in quadrature</td>
<td>5.1%</td>
</tr>
</tbody>
</table>

TABLE II. Michel electron energy spectrum systematic uncertainties estimates from simulation. The uncertainties are expressed with respect to the mean energy of the reconstructed Michel electron energy spectrum.
based on the hit distribution variations. This is the largest systematic contribution in this analysis with a value of 4.0%, originating from the requirement to separate electron from muon hits. A systematic uncertainty of 2.2% is assigned to the recombination factor resulting from the 2% uncertainty on the Modified Box model [36] parameters and the 1% uncertainty based on the electric field variation from the Modified Box model value of 0.481 kV/cm to 0.500 kV/cm in ProtoDUNE. In addition, a test of systematic effects on the use of average constant recombination correction \( R = 0.644 \) for all events was tested in our data-driven method described in Sec. V. When comparing the reconstructed electron energy using \( R \) as an average constant value for all events to the energy using \( R \) applied on an event-by-event basis, a difference of <1.0% was found between the two derived energy scales, which was well within the systematic error assigned to the recombination factor \( R = 0.644 \pm 0.014 \).

For the evaluation of the systematic uncertainty from the difference between Michel electrons and positrons, the impact on the true Michel electron energy spectrum is evaluated by considering both electrons’ and positrons’ energy spectra separately. The systematic uncertainty is evaluated by taking the ratio of the difference between the means of the two distributions of electrons and positrons to the mean of the distribution having both positrons and electrons included. The uncertainty from this systematic contribution is 1.7%. The space charge effect is due to the nonuniformity in the electric field due to the low mobility of heavy Ar ions compared to the electrons in the TPC. To quantify the space charge effect systematic uncertainty, simulated data samples with space charge ON and OFF are evaluated. The systematic uncertainty is estimated by taking the percentage difference in the average value of the reconstructed Michel electron energy spectrum from both samples. The space charge affects the mean value of the Michel electron energy distribution by about 1.4%. In conclusion, the total systematic uncertainty on the absolute Michel electron energy scale is estimated to be 5.1%.

Figure 7 (top) presents the reconstructed Michel electron energy spectrum using the muon-based calibration with ProtoDUNE data (in black points), from MC simulation including both signal and background contributions (in red), and from background only MC events (in blue). The number of MC simulation events is normalized to the number of data events. The data error bars represent the statistical uncertainties. MC simulation error bands include MC statistical and systematic uncertainty contributions added in quadrature. The mean value of the reconstructed Michel electron energy spectra is \( 29.4 \pm 0.2 \) (stat) MeV and \( 28.7 \pm 0.2 \) (stat) \( \pm 1.4 \) (syst) MeV for data and MC simulation, respectively. Relative energy scales of data and MC simulation events agree to within 1.8%. The ratio of data to MC reconstructed energy spectra is flat within statistical and systematic uncertainties. Figure 7 (bottom) shows the reconstructed Michel electron energy spectrum from ProtoDUNE-SP data and simulation (top); Michel electron reconstructed energy using stopping muon calibration versus true Michel electron energy (bottom). Bins having a very low number of events are not shown in this plot.

The results demonstrate that the Michel electron energy spectrum from data is closely reproduced by the theoretically well-understood Michel electron energy distribution when propagated through the detector simulation and reconstruction.

**B. Michel electron calibration to true energy**

This section describes an alternative approach to estimate the reconstructed Michel electron energy spectrum by using the theoretical Michel electron energy distribution. The model applied here assumes a linear relationship between collected charge and reconstructed energy as motivated by the muon-based electron energy reconstruction method described by Eq. (3). The charge collected by the collection plane wires is converted to true Michel electron energy by a calibration procedure in which the true Michel electron energy distribution convolved with a resolution function with parameters that characterize the electron energy resolution is fit to the charge distribution,
using an energy resolution model described later by Eq. (6) and discussed in Sec. VII C. The total reconstructed energy of the Michel electron is given as

$$E = \sum_{i=1}^{N} \frac{dQ_i}{C_{\text{scale}}}$$

(4)

where \(dQ_i\) (in ADC tick) corresponds to the charge deposited in the \(i\)th hit, and \(N\) corresponds to the total number of candidate Michel electron hits. The calibration scale factor, \(C_{\text{scale}}\) (ADC tick/MeV), translates the collected charge to reconstructed Michel electron energy. By using the simulation to relate the true (theoretical) Michel energy spectrum to collected charge, the fit parameters \((C_{\text{scale}} = 95.2 \pm 3.1 \text{ ADC tick}/\text{MeV}, \ p_0 = 0.20 \pm 0.08, \ p_1 = 2.10 \pm 0.08 \text{ MeV}^{1/2}, \ \text{and} \ p_2 = 6.85 \pm 0.29 \text{ MeV})\) are obtained with a Minuit minimization algorithm [38]. This four-parameter approach matches simulated true and reconstructed energy distributions with the best value of \(\chi^2/\text{ndf} = 231/46\). The \(C_{\text{scale}}\) parameter is then applied on an event-by-event basis to the simulation and data to obtain the updated reconstructed Michel electron energy spectrum. This true energy-based fitting procedure with resolution smearing is used to match the reconstructed charge to true energy, while the energy resolution is characterized in Sec. VII C.

Systematic uncertainties in the truth-based energy scale come from the need to convert collected nominal charge to energy, and from the impact of Michel electron and positron content in the true energy spectrum. The corresponding value of the \(C_{\text{scale}}\) was changed by \(\pm 1\sigma\) where \(\sigma\) denotes the statistical uncertainty associated with its value obtained from the fit. Evaluation of the systematic uncertainty from the spectral difference between Michel electrons and positrons is already described above. The uncertainties from these systematic contributions turn out to be 2.9% and 1.7%, respectively. In conclusion, the total systematic uncertainty on the absolute Michel electron energy scale is estimated to be about 3.4%.

Figure 8 (top) presents the reconstructed Michel electron energy spectrum using the true energy-based calibration with ProtoDUNE data (in black points), from MC simulation including both signal and background contributions (in red), and from the background only MC events (in blue). The number of MC simulation events is normalized to the number of data events. The data error bars represent the statistical uncertainties. MC simulation error bands include MC statistical and systematic uncertainty contributions added in quadrature. After correcting the reconstructed charge distributions in data and simulation by the same \(C_{\text{scale}}\) factor, the mean values of the reconstructed Michel electron energy spectra are \(40.4 \pm 0.2\) (stat) MeV and \(39.1 \pm 0.2\) (stat) \(\pm 1.3\) (syst) MeV for data and MC simulation, respectively. The energy scales of data and MC simulation events agree to within 2.6%. The ratio of data to MC reconstructed energy spectra flattens out when the MC energy scale is varied with predicted systematic uncertainties. Figure 8 (bottom) shows the reconstructed Michel electron energy versus the true Michel electron energy distribution. The true energy-based calibration depends on the collected charge only, and is independent of the muon-based calibration constants and of the recombination correction. With the reconstructed charge distribution normalized to directly match the true Michel electron energy distribution smeared with a resolution function, the final reconstructed Michel electron energy distribution does not show the energy offset due to major losses of energy outside the cone and the energy below the hit reconstruction threshold. These losses are incorporated in the value of \(C_{\text{scale}}\). Therefore, the mean of the reconstructed Michel electron energy distribution using the true energy-based calibration method is higher than the one obtained using the muon-based calibration method.
C. Michel electron energy resolution

A proper interpretation of the Michel electron energy resolution requires a complete understanding of the main sources of energy loss. About 24% of the Michel electron energy is lost when using the reconstructed cone-only energy paired with readout threshold effects described in Sec. VI. This is a significant fraction of the energy, and a proper understanding of energy underestimation is very important for DUNE and for other LArTPC experiments. It is appropriate to point out that this amount of Michel electron energy loss was previously observed by other LArTPC experiments, but up to now, no detailed investigation of the causes for lost energy has been reported [13,14].

The fractional energy difference ($\Delta \varepsilon$) per event is defined as

$$\Delta \varepsilon = \frac{(E_{\text{true}} - E_{\text{reco}})}{E_{\text{true}}}$$

(5)

where $E_{\text{true}}$ is the true Michel electron energy and $E_{\text{reco}}$ is the reconstructed Michel electron energy per event. Figure 9 shows various $\Delta \varepsilon$ distributions in the simulation: before the addition of any lost energy contribution, called nominal reconstruction (in red), after the addition of the lost energy outside the reconstructed cone (in blue), and after including the additional contribution of lost energy due to hit reconstruction threshold (in green). The $\Delta \varepsilon$ peak is closer to zero when both lost energy contributions are added, in contrast to the situation before the addition of lost energy components.

For a homogeneous calorimeter such as the ProtoDUNE-SP LArTPC, the energy resolution $\sigma(E)/E$ is expressed by the equation

$$\frac{\sigma(E)}{E} = p_0 \oplus \frac{p_1}{\sqrt{E}} \oplus \frac{p_2}{E}$$

(6)

where $\sigma(E)/E$ is the standard deviation in the reconstructed Michel electron energy divided by the true Michel electron energy distribution in energy bins (shown in Fig. 10) and $E$ is the mean of the reconstructed Michel electron energy distribution obtained in each true energy bin. The terms on the right-hand side are the constant term ($p_0$), the stochastic term ($p_1/\sqrt{E}$), and the noise term ($p_2/E$). The operator $\oplus$ indicates a sum in quadrature. The constant term describes the resolution losses due to lost energy. The stochastic term incorporates contributions to the energy resolution from the statistical fluctuations in the number of ionization electrons and scales as $1/\sqrt{E}$. The noise term accounts for the electronic noise of the collection wires and readout electronics ADCs and scales as $1/E$.

The Michel electron energy resolution distributions are shown as a function of true Michel electron energy in Fig. 10. The x-axis points represent the mean values of the Michel electron true energy bins, and the horizontal error bars correspond to the standard deviation of each true
Michel electron energy bin; the statistical uncertainty on the fit to $\sigma(E)/E$ values [from Eq. (6)] is shown along the vertical axis. Table III presents the mean values of the Michel electron energy for various samples as well as the values obtained for the parameters in Eq. (6), as obtained from a least-squares fit.

Constant and stochastic terms are affected by the resolution losses due to the lost energy. Assuming the lost energy contributions described in the MC study (Sec. VI) are added back to the energy balance, the resolution improves, as quantified in Table III. Figure 10 shows the energy resolution fit [Eq. (6)] applied to both muon-based and true energy-based calibrated Michel electron energy with the results consistent within the statistical uncertainties. The energy resolution of $\sim$40% is derived at 50 MeV when using the nominal (i.e. without lost energy recovered from the MC) muon-based calibration method. If the lost energy contributions from outside the cone and energy below hit reconstruction threshold are added, the resolution improves relative to the nominal case: the constant term becomes very small, and the resolution becomes limited by the stochastic term from about 50 MeV energy. For parameters in Table III the correlation coefficients are consistent between muon-based and true energy-based calibration methods with the constant term $p_0$ being highly anticorrelated with the stochastic term $p_1$. The following observations can be made:

(i) In the nominal cosmic muon-based calibration, the collected (visible) charge is corrected by calibration constants and converted to reconstructed energy. Since the mean of the true Michel electron energy spectrum is at 38.4 MeV, the nominal energy reconstruction recovers $\sim$75% of the total deposited energy.

(ii) The energy resolution constant term ($\sim$26%) describes the resolution losses due to the lost energy. In the MC simulation, it is possible to add the lost energy to the reconstructed energy balance. In this case, the energy resolution drops from about 40% to 25% at 50 MeV. The lost energy recovery is not possible in the collected data set with the existing charge readout threshold and applied selection (cone cut) optimized to reduce backgrounds.

(iii) If the lost energy is accounted for, as performed in the simulation, the stochastic term decreases from 1.91 to about 1.24. The stochastic term described here may suggest that the energy resolution at a few percent level might be achievable for the DUNE far detector in the few GeV electron neutrino energy range, assuming negligible lost energy and noise contributions to the resolution. These potential improvements would have important implications for low-energy electrons expected for supernova neutrinos, and also for the few GeV scale electrons to be observed in the DUNE far detector from $\nu_\mu \rightarrow \nu_e$ oscillation.

(iv) In the 10–50 MeV energy range relevant to solar or supernovae measurements, the noise term currently dominates. In order to improve the sensitivity of these measurements, one needs to improve understanding of the noise effects.

(v) By construction, the true energy-based Michel electron reconstruction is in good agreement with the theoretical Michel electron energy as presented in Fig. 8. As a consequence, the mean values of the Michel electron energy distribution in data (40.4 MeV) and in MC simulation (39.1 MeV) are in close agreement with the theoretical Michel electron energy spectrum with the mean at 38.4 MeV. The method does not recover the energy resolution loss but accounts for the average lost energy.

VIII. SUMMARY

This article describes the event selection and energy reconstruction of low-energy electrons in the DUNE prototype ProtoDUNE-SP LArTPC. A high-purity (95%) Michel electron event sample is selected and used to calibrate the electron energy scale, and to quantify the effects of the detector response to low-energy electrons including readout electronics threshold effects. The event selection techniques for cosmic ray muons and Michel electrons have been developed. The selected Michel
electron sample was used to verify the recombination correction factor and the data and MC simulation agreement was presented based on the Modified Box recombination model.

Two complementary energy reconstruction techniques to calibrate the Michel electron energy spectrum are described. The “cosmic-muon” based calibration is based on a model-dependent recombination correction and relies on the calibration constant derived from cosmic ray muon measurements. On the other hand, the “true-energy” based calibration method is based on the theoretical Michel energy spectrum and is independent of any correction applied in the muon-based energy reconstruction. An excellent agreement between data and simulation for the Michel electron energy spectrum to within 2% and 3% using muon-based calibration and the true energy-based Michel electron calibration, respectively, have been observed. Once a sample of the low-energy electrons is collected in the far detector, it will be calibrated to its true energy by converting reconstructed visible energy based on the relationship presented in Fig. 7 (bottom) for the muon-based method and Fig. 8 (bottom) for the true-based calibration method. The two methods will cross-check each other and may quantify a lost energy. As part of this analysis, the estimates for systematic uncertainties on the Michel electron energy spectrum are presented. The dominant contribution to the systematic uncertainty comes from the difference in the hit association effects close to the candidate muon end position in the data and simulation.

This article also reports the sources of the lost energy and quantifies the effect of each of those sources separately. The lost energy coming from charge readout threshold effects and from the event selection is evaluated to be about 11% and 13%, respectively. The energy resolution is quantified in this analysis. In the nominal “cosmic-muon” based calibration, the collected charge is corrected by calibration constants and converted to reconstructed energy. While the mean of the true Michel electron energy spectra is at 38.4 MeV, the nominal energy reconstruction mean is at 28.7 MeV due to the lost energy effect. After the addition of the lost energy in MC, the constant term approaches zero, and the stochastic resolution term improves by 35%. In such a case the energy resolution improves from about 40% to 25%, at 50 MeV. Assuming the lost energy is fully recovered with negligible noise contributions, the DUNE far detector may reach the energy resolution defined by the stochastic term alone [Eq. (6)], consistent with low-energy physics goals of DUNE [4] and other LArTPCs [17]. These results demonstrate the capabilities of the ProtoDUNE-SP (and ultimately the DUNE far detector) to detect and reconstruct electrons with energies up to ~50 MeV.

For further improvements it will be important to understand if the charge collection in the DUNE far detector can operate at lower thresholds and noise levels to further improve the energy resolution. The DUNE far detector data will be dominated by single muon and electron events, where the electron event selection and reconstruction efficiencies will improve in the absence of nearby cosmic ray background activity. As a result the event selection will be further optimized for the DUNE far detector analyses. Understanding of energy resolution and its potential improvements will have important implications for electrons from \( \nu_e \) interactions in the DUNE far detector. Analysis of low-energy neutrino interactions in DUNE will benefit from a combination of muon-based energy calibration, Michel electron true energy-based calibration, and detailed MC modeling to characterize the energy resolution with potential energy losses.

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