

#### **On-The-Fly Interpolation for Thermal Scattering in MCS**

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- Resolved resonance energy range
  - Windows Multipole
  - Target Motion Sampling
  - Interpolation
  - SIGMA1
  - Gauss-Hermite

#### **Doppler Broadened Cross-section**

$$\overline{\sigma}(v) = \frac{\alpha^{1/2}}{\pi^{1/2} v^2} \int_0^\infty \sigma(V) V^2 \left\{ e^{-\alpha(V-v)^2} - e^{-\alpha(V+v)^2} \right\} dV$$





- In the unresolved energy range
  - Average and variance of resonance parameters are given
  - Interpolation
  - Sampling Resonance Parameter

Probability distribution for total cross section at 20 keV



Absorption cross section of <sup>235</sup>U, <sup>238</sup>U and <sup>135</sup>Xe

#### Thermal Scattering (bond scattering)

#### Interpolation

- Makxsf (from MCNP)
- LEAPR (NJOY)

Distribution of outgoing energy with incident energy of 0.115 eV for H in  $H_2O$ . (black = 51.3 deg, red = 60 deg, green = 68 deg)





#### MCS OTF cross-section treatment

#### Unresolved resonance energy range

- Windows multipole
- SIGMA1 (ongoing)
- Interpolation

#### Probability-table

Interpolation

### Thermal scattering

Interpolation

# **On-The-Fly Interpolation**





- MCS follows Makxsf interpolation scheme
- Makxsf is utility program for manipulating cross-section library for MCNP5
  - Doppler broadening for resolved resonance data by SIGMA1 kernel
  - Interpolation of unresolved resonance probability-table data
  - Interpolation of  $S(\alpha,\beta)$  thermal scattering data

#### Interpolation scheme used for Unresolved resonance range

- ACE format outgoing information is not temperature dependent
- Log-lin interpolation for cross-section

$$\sigma(T) = f \cdot \sigma(T_{low}) + (1 - f) \cdot \sigma(T_{high}) \qquad f = \frac{\ln(T_{high}) - \ln(T)}{\ln(T_{high}) - \ln(T_{low})}$$



#### **On-The-Fly Interpolation**

- Interpolation scheme used for Thermal Scattering Data
  - Lin-lin interpolation for cross-section
  - Lin-Lin interpolation for outgoing angle
  - Reverse lin-lin interpolation for outgoing energy
    - Outgoing energy distribution is reversely proportional to temperature

$$f = \frac{T_{high} - T}{T_{high} - T_{low}} \qquad E_{out} = \left(\frac{f}{E_{low}} - \frac{1 - f}{E_{high}}\right)^{-1}$$

- The energy and angle are depends on
  - Incoming energy
  - Random number (0, 1]
- Grid will be different for different temperature

# OTF interpolation can be implemented by using existing kernel

**Algorithm** OTF interpolation collision kernel  $f = (T_{high} - T)/(T_{high} - T_{low})$ seed0 = get\_random\_seed  $[E_{low}, uvw_{low}] =$ collision\_kernel  $(D_{low})$ change\_seed(seed0)  $[E_{high}, uvw_{high}] =$ collision kernel  $(D_{high})$  $E_{out} = 1/(f/E_{low} + (1-f)/E_{high})$ if (GetRN() < f) $uvw_{out} = uvw_{low}$ else  $uvw_{out} = uvw_{high}$ end if

# Verification



#### INDC Benchmark VERA-1C PMR Compact



- INDC Benchmark
  - Pin cell benchmark designed to test thermal scattering capability
  - Pure water with density of 1g/cm<sup>3</sup>
  - Temperatures of all regions are 293.6K

Case	ZA	Density (#/barn-cm)
4 (0)	92235	4.6614E-04
1/2" pin	92238	4.7099E-02
1/4″ pin	92235	1.6653E-03
	92238	4.5915E-02
	92235	3.3589E-02
1/8" pin	92238	1.4395E-02



5.08 cm

D.E. Cullen, R.N. Blomquist, C. Dean, et al., "How Accurate Can We Calculate Thermal Systems?," INDC(USA)-107, International Nuclear Data Committee, 2004

#### • Verification of MCS S( $\alpha$ , $\beta$ )

Case	MCNP	SD	MCS	SD	Diff. (pcm)
1/2″ no S(α,β)	1.01649	0.00004	1.01658	0.00004	-9
1/2″ S(α,β)	0.96812	0.00004	0.96806	0.00004	6
1/4″ pin no S(α,β)	1.01320	0.00016	1.01359	0.00017	-39
1/4″ pin S(α,β)	0.92197	0.00017	0.92214	0.00019	-17
1/8″ pin no S(α,β)	1.01320	0.00021	1.01327	0.00024	-7
1/8" pin S(α,β)	0.90950	0.00021	0.90895	0.00023	55

Flux Spectrum of ½" pin



- For the Test the temperature has changed to 600K
  - Since thermal scattering data of light water exist from 293.6K
- Three cases (half inch problem)
  - NJOY: 600K thermal scattering data processed by NJOY
  - Mkaxsf: 600K data interpolated using 550K and 650K by makxsf
  - OTF: OTF interpolation using 550K and 650K data
- # of nuclides = 4

Case	k <sub>eff</sub>	SD	Diff. (pcm)	Time
NJOY	1.00757	0.00001	-	1.00
Makxsf	1.00743	0.00001	-14	1.01
OTF	1.00741	0.00001	-16	1.14

# Relative error of flux spectrum and 2sigma standard deviation



## **VERA-1C Benchmark**

- VERA-1C benchmark
  - Fuel temperature is 900K
  - Others are 600K
  - # of nuclides = 40
  - All nuclides are treated with same ACE files but lwtr thermal scattering data
    - NJOY: with 600K data processed by NJOY
    - Makxsf: with 600K data interpolated using 550K and 650K data by Makxsf
    - OTF: OTF interpolation using 550K and 650K data





#### **VERA-1C Benchmark**

Case	$\mathbf{k}_{\mathbf{eff}}$	SD	Diff. (pcm)	Time
NJOY	1.17402	0.00012	-	1.00
Makxsf	1.17414	0.00011	12	0.99
OTF	1.17402	0.00013	0	1.01

#### Relative error of flux spectrum in coolant region



## **PMR-200 Compact**

#### • PMR-200 compact with 23.5% packing fraction

- 1000K is used for all regions
- All nuclides are treated with same ACE files but graphite thermal scattering data
  - NJOY: with 1000K data processed by NJOY
  - Makxsf: with 1000K data interpolated using 800K and 1200K data by Makxsf
  - OTF: OTF interpolation using 800K and 1200K data





### **PMR-200 Compact**

Case	$\mathbf{k}_{eff}$	SD	Diff. (pcm)	Time
NJOY	1.28546	0.00004	-	1.00
Makxsf	1.28551	0.00004	5	1.00
OTF	1.28555	0.00004	9	1.02

#### Relative error of flux spectrum in coolant region



# On-The-Fly Interpolation For Probability-Table





#### **OTF Interpolation**

Log-lin interpolation scheme

$$\sigma(T) = f \cdot \sigma(T_{low}) + (1 - f) \cdot \sigma(T_{high}) \qquad f = \frac{\ln(T_{high}) - \ln(T)}{\ln(T_{high}) - \ln(T_{low})}$$



#### Algorithm OTF interpolation of ptable

$$f = (\ln(T_{high}) - \ln(T))/(\ln(T_{high}) - \ln(T_{low}))$$
  
seed0 = get\_random\_seed  
$$XS_{low} = get_xs (D_{low})$$
  
change\_seed(seed0)  
$$XS_{high} = get_xs (D_{high})$$
  
$$XS = f XS_{low} + (1-f)XS_{high})$$



# Summary





#### On-The-Fly Interpolation Function is implemented

#### Thermal scattering

- Lin-lin for cross-section
- Lin-lin for outgoing angle
- Reverse lin-lin for outgoing energy

#### • Probability-table

- Log-lin for cross-section
- Cross-sections
  - Sqrt-lin for cross-section

#### OTF function is tested on

• INDC pin, VERA-1C, PMR-200 compact

#### OTF XS matches well with Makxsf while the computing cost is negligible