# A Direct Numerical Simulation Study of Turbulent Hydrogen Jet Flames with Different Coflow Air Temperature 

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#### Abstract

The properties of turbulent lifted non-premixed hydrogen jet flames under different coflow air temperature have been analyzed due to their relevance to practical applications. Three dimensional direct numerical simulations of turbulent lifted hydrogen/air jet flames were conducted to examine the flame structure and stabilization mechanisms of turbulent lifted jet flames. Chemical explosive mode analysis (CEMA) reveals the important variables and reactions for stabilizing the lifted flames. The high coflow air temperature DNS case shows that auto ignition is the main source of stabilization mechanism of the lifted flame. On the other hand, the case of low coflow air temperature indicates that flame propagation is the dominant stabilization mechanism of lifted jet flame.


KEYWORDS: DNS, Hydrogen jet flame, Chemical explosive mode analysis, Stabilization mechanism

## 1. INTRODUCTION

The characteristics of turbulent lifted non-premixed jet flames under various coflow conditions have widely been investigated due to their relevance to practical applications such as diesel engines, gas turbine combustors, and commercial boilers. In addition, the stabilization mechanisms of turbulent lifted jet flames are so complex. In many practical devices, ambient air around fuel jet is hot enough to induce auto-ignition of fuel/air mixture upstream of the flamebase. As such, auto-ignition has been found as the primary stabilization mechanism of turbulent lifted flames in hot vitiated coflows. Previous 3-D direct numerical simulations (DNSs) of hydrogen [2] and ethylene [3] jet flames in highly-heated coflows showed that turbulent lifted jet flames are stabilized by the auto-ignition of fuel-lean mixtures supported by the hot coflow temperature exceeding the auto-ignition limit and are also determined by the balance between the local axial velocity and consecutive auto-ignition events occurring in hot fuel-lean mixtures.
However, the stabilization mechanism of turbulent lifted jet flames in mildly-heated coflows of which temperature is near auto-ignition limit has not been extensively investigated, even though the overall characteristics of such flames were reported in experimental studies [4,5]. From these experiments, it was found that the lift-off height correlates well with the inlet jet velocity based both on the premixed flame theory and the large eddy theory regardless of the inlet temperatures. For the large eddy theory, however, the thermal diffusivity evaluated at the inlet temperature rather than at the burnt gas temperature is adopted to obtain a proper correlation. In this study, three 3-D DNSs of turbulent lifted hydrogen/air jet flames in heated coflows near auto-ignition limit are performed to examine the stabilization mechanisms and flame structure of turbulent lifted jet flames.

## 2. PROBLEM CONFIGURATION

Three different direct numerical simulations (DNSs) of spatially-developing turbulent lifted jet flames were performed in a 3-D slot-burner configuration. Fuel issues from a central jet, which consists of $65 \%$ hydrogen and $35 \%$ nitrogen by volume at an inlet temperature of $T_{j}=400 \mathrm{~K}$. The central jet is surrounded on either side by co-flowing heated air streams at three different temperatures of $T_{c}=750$ (Case L), 850 (Case M), and $950 \mathrm{~K}(\mathrm{Case} \mathrm{H})$ and atmospheric pressure. The fuel jet and coflow velocities are specified as $U_{j}=240 \mathrm{~m} / \mathrm{s}$ and and $U_{c}=2 \mathrm{~m} / \mathrm{s}$, respectively. The fuel jet width, $H$, is 2 mm such that the jet Reynolds number, $R e_{j}=U_{j} H / v$, is approximately 8000 . The computational domain is $15 H \times 20 H \times$ $3 H$ in the streamwise, $x$, transverse, $y$, and spanwise, $z$, directions with $2000 \times 1600 \times 400$ grid points. A uniform grid spacing of $15 \mu \mathrm{~m}$ is used in the x and z -directions, while an algebraically stretched mesh is used in the $y$-direction as in [1].
The compressible Navier-Stokes, species continuity, and total energy equations were solved using the Sandia DNS code, S3D, with a 4th-order Runge-Kutta method for time integration and an 8th-order central differencing scheme for spatial discretization. A detailed hydrogen/air kinetic mechanism was adopted for DNSs [2]. Improved nonreflecting inflow/outflow boundary conditions [3,4] were used in the x and y -directions and periodic boundary conditions were applied in the homogeneous z -direction. Based on the fuel jet velocity and the streamwise domain length, a flow-through time, $\tau_{j}=L_{x} U_{j}$, is 0.125 ms . Note that the steady lift-off heights are found to be approximately $\bar{h}_{H} / H=2.4, \bar{h}_{M} / H=4.0$, and $\bar{h}_{L} / H$ $=5.3$. Figure 1 shows 3-D volume-rendering of the mass fraction of OH and $\mathrm{HO}_{2}$ at $t / \tau_{j}=2.0$.


Fig. 1 3-D volume rendering of OH and $\mathrm{HO}_{2}$ mass fractions of turbulent lifted hydrogen jet flames for Cases L, M, and H (from left to right)

## 3. ANALYSIS

Chemical explosive mode analysis (CEMA) is adopted to further identify the characteristics of the lifted flamebases [5,7]. CEMA is briefly introduced here and for more details of it, refer to [5,6]. The differential equations of a typical reacting flow can be described in discretized form as equation 1:

$$
\begin{equation*}
\frac{D \mathbf{y}}{D t}=\mathbf{g}(\mathbf{y})=\boldsymbol{\omega}(\mathbf{y})+\mathbf{s}(\mathbf{y}) \tag{1}
\end{equation*}
$$

where $D / D t$ is the material derivative and $\mathbf{y}$ represents the solution vector of species concentrations and temperature. The chemical source term is denoted as $\boldsymbol{\omega}$, while all non-chemical source terms such as diffusion in flames and homogeneous mixing term in stirred reactors are represented by $\mathbf{s}$.
CEM is defined as a chemical mode of which real part of the eigenvalue, $\lambda_{e}$, is positive. CEM represents the reciprocal chemical time scale of a local mixture and as such, the existence of CEM implies that the corresponding mixture is explosive in nature.

In nonpremixed turbulent flames, the loss of heat and radicals can be characterized by the mixing or scalar dissipation rate, $\chi$, which is defined by $\chi=2 D|\nabla \xi|$, where $D$ is local thermal diffusivity. The competition between the CEMs and the loses can approximately be quantified by a Damköhler number defined by $D a_{c}=\lambda_{e} \cdot \chi^{-1}$. Note that mixture with $D a_{c} \gg 1$ indicates a dominant CEM which will be likely to result in actual ignition; otherwise ignition may be suppressed by the losses.


Fig. 2 Isocontours of $\operatorname{sign}\left(\lambda_{\mathrm{e}}\right) \times \log _{10}\left(\max \left(1,\left|D a_{\mathrm{c}}\right|\right)\right)$ for Cases $\mathrm{L}, \mathrm{M}$, and H (from left to right). White lines denote the flamebase with $\boldsymbol{D} \boldsymbol{a}_{\boldsymbol{c}}=\mathbf{1}$.

Figure 2 shows isocontour of $D a_{c}$ in $\log$ scale for the cases. Note that a large positive $D a_{c}$ in red indicates that the CEM dominates the mixing process such that the mixture is auto-igniting. A large negative $D a_{c}$ in blue, however, indicates fast reacting post-ignition mixture such that its overall reaction progress can be limited by the slower local transport process. As such, the dark blue regions in Fig. 2 contain diffusion flame kernels. It is also readily observed that for Case H, there exist two strips of autoigniting mixtures (red) upstream of the flamebase, leading to ignited mixtures (blue). This result verifies that the stabilization mechanism of Case H is auto-ignition. In Cases L and M , however, large positive $D a_{c}$ occurs only at narrow regions right upstream of the flamebase, which corrspond to the preheated zone of a premixed flame. This result verifies that turbulent lifted flames for Cases L and M are mainly stabilized by flame propagation whereas the stabilization of the lifted flame for Case H is primarily attributed to auto-ignition of fuel-lean mixtures upstream of the flamebase.

The physicochemical characteristics of the flames are further investigated using the explosion index (EI) and participation index (PI), which represent the contribution of variables and reactions to CEM, respectively. The EI and PI vectors are defined as equation 2 [5,6]:

$$
\begin{equation*}
\mathbf{E I}=\frac{\left|\mathbf{a}_{e} \otimes \mathbf{b}_{e}^{T}\right|}{\sum\left(\left|\mathbf{a}_{e} \otimes \mathbf{b}_{e}^{T}\right|\right)^{\prime}} \quad \mathbf{P I}=\frac{\left|\mathbf{b}_{e} \cdot \mathbf{S} \otimes \mathbf{R}\right|}{\sum\left(\left|\left(\mathbf{b}_{e} \cdot \mathbf{S}\right) \otimes \mathbf{R}\right|\right)^{\prime}} \tag{2}
\end{equation*}
$$



Fig. 3 EI-weighted color-mixing contours of temperature (red), $\mathrm{H}_{2}$ (blue), H (green), O (cyan), and $\mathrm{O}_{2}$ (yellow) for Cases L, M, and H.White lines denote the flamebase with $D a_{c}=1$.

Figure 3 shows EI-weighted color-mixing contours of important variables to the CEM. For all cases, temperature is found to be the most important variable right upstream of the flamebase. This is because temperaure becomes significant to a CEM in the preheated zone of premixed flame. Unlike Cases L and M , however, O and OH radicals are found to be important in the auto-igniting layers that can stabilize the lifted flame in Case H. Moreover, two important reactions that control the auto-igniting layer are R1 and R9. This is because R1 and R9 are two competing reactions determining the 2nd explosion limit of $\mathrm{H}_{2} / \mathrm{O}_{2}$ mixture. It is also of interest to note that even in the preheated zone of Case L \& M, and thermal ignition layer of Case H where temperature governs the CEM, R1 and R9 are also found to be the two most important reactions to the CEM. It is primarily because R9 is one of the major heat release reactions and R 1 is the major endothermic reaction in both premixed and non-premixed $\mathrm{H}_{2} /$ air flames.
In the lean mixtures of the lifted flames, $\mathrm{H}_{2}$ becomes important to the CEM; however, in the rich mixtures of the flames, H becomes critical to rich premixed flame. From PI analysis (see Table 1), it is readily observed that in the lean mixtures (Point 1), two major heat release reactions, R3 and R9 are identified as the most important reactions to the CEM. In the rich mixtures (Points 3 and 5), however, R8 and R9 are found critical to the CEM. It is also of importance to note that near the stoichiometric mixtures (Point 2), O and H are important EI species and R9 \& R8 are the critical PI reactions.


Fig. 4 PI-weighted color-mixing contours of R1 (red), R2 (green), R3 (blue), R9 (yellow), and R10 (cyan) for Cases L, M, and H . White lines denote the flamebase with $D a_{c}=1$.

Figure 4 shows the selective PI of R1 to R10 of each case. PI of R10 $\left(\mathrm{HO}_{2}+\mathrm{H}=\mathrm{H}_{2}+\mathrm{O}_{2}\right)$ forks at the upstream of flame base for Cases M and H , although its value is relatively small in Case M. A hook shaped PI for R9 appears occasionally at the right upstream of flamebase in Case M, while it sticks every time on the flame base for case H .
$\mathrm{R} 1, \mathrm{R} 2\left(\mathrm{O}+\mathrm{H}_{2}=\mathrm{H}+\mathrm{OH}\right)$ and R 3 are the important chain branching reactions on flame propagation [8]. The shape of PI for R1 and R3 near downstream of flamebase exhibits nearly the same for both Cases L and M . The only difference is that in Case M, PI of R1 sometimes appears near downstream of white solid $D a_{c}$ line like Case H where PI of R1 is always important immediately downstream of flamebase.
Case M have the characteristics of both flame propagation and auto-ignition near flamebase from a point of view of the behavior of PI. It can be conjectured that the stabilization mechanism for Case M is a mixed mode of auto-ignition and flame propagation in a qualitative manner.
The characteristics of stabilization mechanism and flame structure of turbulent lifted hydrogen jet flames in heated coflow at three temperatures of 750,850 and 950 K near auto-ignition limit were investigated with a detailed $\mathrm{H}_{2} / \mathrm{O}_{2}$ mechanism. Overall flame structure and chemical explosive mode analyses revealed that auto-ignition is the main stabilization mechanism of the lifted jet flame for Case H and flame propagation is the main stabilization mechanism for Case L . The mixed mode of auto-ignition and flame propagation is found to be the main stabilization mechanisms for Case M from qualitative PI analysis. For all cases, T and $\mathrm{H}_{2}$ are important variables in the preheated zone and thermal ignition layer upstream of the flamebase, where R1 and R9 are found the most importance reactions to the CEM.

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